

From: Maccone, L. (2013). "A simple proof of Bell's inequality". [arxiv.org/pdf/1212.5214.pdf](https://arxiv.org/pdf/1212.5214.pdf)

We use the apparatus and method of the modal logic model checker Meth8/VL4, a resuscitation and correction of the modal logic system of Łukasiewicz B<sub>4</sub>.

The designated *proof* value is  $\top$  tautology; other values are:  $\mathbb{N}$  truthity (non contingency);  $\mathbb{C}$  falsity (contingency); and  $\mathbb{F}$  contradiction.

With four propositional variables, the 16-valued truth table result is row-major and horizontal.

LET  $\sim$  Not;  $\&$  And;  $+$  Or, add;  $>$  Imply, greater than;  $<$  Not Imply, less than;  
 $=$  Equivalency;  $\%$  possibility, for one or some;  $\#$  necessity, for all;  
 $p$  probability;  $(\%p\>\#p)$  ordinal one,  $\mathbb{N}$  truthity;  $(p=p)$   $\top$  tautology, theorem;  
 $\sim(x>y)$  not (x greater than y), as in x equal to or less than y.

The summation of the respective probabilities for q equivalent to r, r equivalent to s, and q equivalent to s is equal to or greater than one, and hence is equivalent to a theorem. (1.1)

$$\sim(\underbrace{((p\&q)=(p\&r))}_{\mathbb{N}\mathbb{N}\mathbb{N}\mathbb{N}} + \underbrace{(((p\&r)=(p\&s))}_{\mathbb{N}\mathbb{N}\mathbb{N}\mathbb{N}} + \underbrace{((p\&q)=(p\&s))}_{\mathbb{N}\mathbb{N}\mathbb{N}\mathbb{N}})) < (\%p\>\#p) = (p=p) ; \tag{1.2}$$

For further qualification to strengthen Eq. 1.1, we rewrite it as:

If the respective probabilities for q, r, s are equivalent to and equal to one, then the summation of the respective probabilities for q equivalent to r, r equivalent to s, and q equivalent to s is equal to or greater than one. (2.1)

$$\underbrace{(((p\&q)=(p\&r)=(p\&s)))}_{\mathbb{N}\mathbb{N}\mathbb{N}\mathbb{N}} = (\%p\>\#p) > \sim(\underbrace{((p\&q)=(p\&r))}_{\mathbb{N}\mathbb{N}\mathbb{N}\mathbb{N}} + \underbrace{(((p\&r)=(p\&s))}_{\mathbb{T}\mathbb{T}\mathbb{N}\mathbb{N}} + \underbrace{((p\&q)=(p\&s))}_{\mathbb{T}\mathbb{T}\mathbb{N}\mathbb{N}})) < (\%p\>\#p) ; \tag{2.2}$$

Eqs. 1.2 and 2.2 as rendered are *not* tautologous. Hence, Bell's inequality as Eqs. 1.1 or 2.1 is refuted.